



Early Journal Content on JSTOR, Free to Anyone in the World

This article is one of nearly 500,000 scholarly works digitized and made freely available to everyone in the world by JSTOR.

Known as the Early Journal Content, this set of works include research articles, news, letters, and other writings published in more than 200 of the oldest leading academic journals. The works date from the mid-seventeenth to the early twentieth centuries.

We encourage people to read and share the Early Journal Content openly and to tell others that this resource exists. People may post this content online or redistribute in any way for non-commercial purposes.

Read more about Early Journal Content at <http://about.jstor.org/participate-jstor/individuals/early-journal-content>.

JSTOR is a digital library of academic journals, books, and primary source objects. JSTOR helps people discover, use, and build upon a wide range of content through a powerful research and teaching platform, and preserves this content for future generations. JSTOR is part of ITHAKA, a not-for-profit organization that also includes Ithaka S+R and Portico. For more information about JSTOR, please contact support@jstor.org.

From $bc - f^2 = a$ a positive quantity, or $ca - g^2 = a$ a positive quantity, it is readily seen that c is positive.

Also solved by H. V. Spunar and G. B. M. Zerr.

GEOMETRY.

330. Proposed by J. J. QUINN, Ph. D., New Castle, Pa.

A line pivoted at the origin revolving with a constant angular velocity, intersects another moving parallel to the Y -axis with a constant linear velocity. (1) Find the locus of their intersection when the ratio of their velocities is as $m:n$ referred to a quadrant and a radius, respectively. (2) Assume $m=3$ and $n=2$, and apply to the trisection of an angle. (3) Under what conditions will this curve become a quadratrix? (4) Name the curve.

Solution by H. V. SPUNAR, M. and E. E., East Pittsburg, Pa.

The angular velocity of the intersection point P , due to the rotation of the radius vector ρ , is constant, say $v_1 = d\theta/dt$, and that linear due to the constant velocity of the moving line in the direction of X -axis is $v_2 = dx/dt$.

(1) Assuming the ratio of the velocities $v_1/v_2 = m/n$, the locus of the point P is

$$\frac{m}{n} = \frac{dv}{dx}, \text{ or } X = \frac{n}{m}\theta + \theta_1.$$

Letting the starting point be the origin, we have in polar coordinates,

$$\rho \cos \theta = \frac{n}{m}\theta.$$

The curve may be applied without any difficulty to the multisection as well as to the trisection of an angle.

(2) To apply the curve " $\rho \cos \theta = 2(\theta/3)$ " to the trisection of the given angle θ . Draw OP at an angle θ (*i. e.*, the angle to be trisected) and PP_1 perpendicular to X -axis; then $OP_1 = \rho \cos \theta = 2(\theta/3) = x_1$; since putting $\theta = 3\phi$, $\rho \cos 3\phi = 3[2(\theta/3)] = 3x_1$. Trisecting the linear abscissae $OP_1 = x_1$, and erecting at $Q_1(x_1/3)$, the perpendicular to the X -axis, cutting the curve at Q , then drawing QO , we obtain $\angle QOX = \phi = (\theta/3)$.

(3) Let in $r \sin \phi = n\phi$ (Dinostrates' Quadratrix), $\phi = (\frac{1}{2}\pi - \theta)$ = the complement of the angle θ . Then $\rho \cos \theta = \frac{n}{m} \left(\frac{\pi}{2} - \theta \right)$.

(4) Hence the name of the curve may be Complementary Quadratrix.

Also solved very neatly by G. B. M. Zerr.

331. Proposed by C. N. SCHMALL, New York City.

The center of two spheres radii r_1, r_2 , are at the extremities of a straight line $2a$ on which as a diameter a circle is described. Find a point on the circumference from which the greatest portion of spherical surface is visible.